

# FAULT TREE ANALYSIS (OVERVIEW FOR ASSE)

EXPERIMENTAL OPERATIONS  
SANDIA NATIONAL LABORATORIES  
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**Thanks to Kevin J. Maloney**

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**References:**

**NST416**

**NUREG0492**

**Relex**

**NASA Fault Tree Handbook**

# OUTLINE

- Origin of Fault Tree Analysis
- Uses for Fault Trees
- Fault Tree Terminology
  - ▶ Faults and Failures
  - ▶ Symbols
  - ▶ Structure
  - ▶ Results
- FTA example
  - ▶ Structure
  - ▶ Boolean Algebra
  - ▶ Results
    - Cut sets
    - Importance levels
- Thermal Test Simple Example
- FTA Results



# HISTORY OF FTA

- Developed by H. Watson and Allison Mearns of Bell Labs for use on the Minute Man Guidance System in 1962
- Boeing expanded its use to the MMII and their own civilian aircraft by 1966
  - ▶ D.F. Hassl
- Codified for use by the FAA in 10CFR25.1309 by 1970
- NRC Fault Tree Handbook, NUREG-0492, in 1975.
  - ▶ Expanded use for PRA after TMI in 1979
- Sandia: Set Equation Transformation System (SETS), 1977
- OSHA codified its use in 19CFR1910.119 after Bhopal and Piper Alpha accidents (1984-1992) for Process Hazard Analysis
- Accepted for use in several international industrial and military standards
  - ▶ MIL-HDBK-338
  - ▶ NASA
  - ▶ International Electrotechnical Commission

# SNL USES FOR FAULT TREES

## Weapon Systems

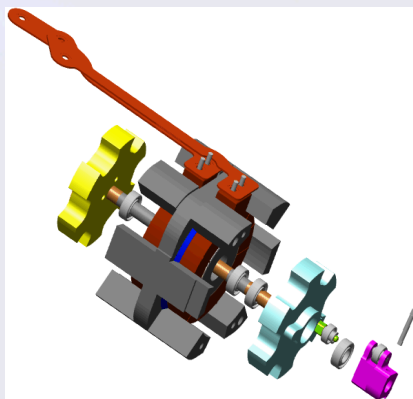


- Weapon Development Phases
- Safety-critical feature identification and configuration management
- Nuclear Weapon Safety Assurance and Assessment

## Testers



## Weapon Components



## Nuclear Reactor Safety



## Other:

- *Human Factors*
- *Reliability*
- *WP&C ES*



# FAULT TREE ANALYSIS - DEFINITION

## ● Fault tree analysis is...

- ▶ A deductive *analytical* technique...
- ▶ whereby an *undesired state* of a system is specified...
- ▶ the system is then analyzed in the context of its *environment and operation*...
- ▶ to find all *credible ways* in which the undesired system state can occur

**A Top-down approach**

**NUREG -0492**

# WHY BUILD A FAULT TREE?

## Qualitative (Most important for us)

- Identify combinations of system failures
  - ▶ Find 'First-Order' Faults
  - ▶ "Single-Point Failures" (WP&C Criteria for Safe Design and Operations, MN471021)
- Identify critical components, procedures, and tasks
- Design aid
- Understanding what you are depending on for safety in your system – engineered controls, administrative controls, PPE, etc.

## Quantitative (Active Safety or for Reliability analysis)

- System unavailability
- Frequency/probability of undesired event

# FAULTS VERSUS FAILURES

## Fault

- The occurrence or existence of an undesired state for a component, subsystem, or system
  - ▶ Example: Solenoid propane valve temporarily freezes open or closed
- Sneak circuits (electrical, pneumatic, hydraulic) are faults – nothing failed, just an unintended, unexpected, response.

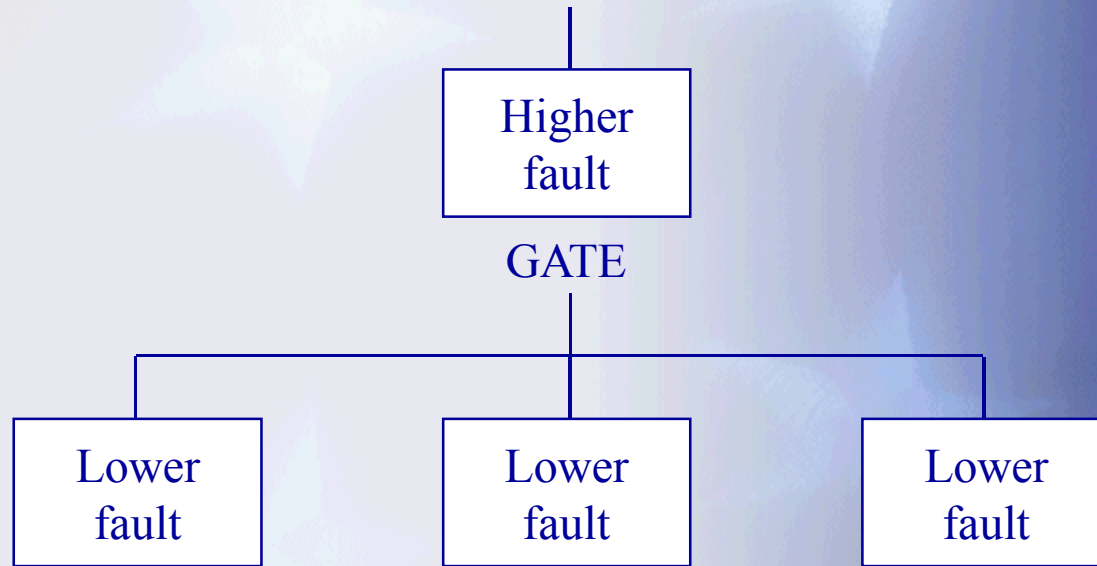
## Failure

- Basic abnormal event that renders a component, subsystem, or system incapable of performing its intended function
- Represented by primary events on a fault tree
  - ▶ Example: Hose breaks

***All failures are faults, but not all faults are failures***



# FAULT TREE GATE FUNCTION



- Fault tree is constructed by proceeding from the higher (general) to the lower faults (specific)
- Inputs (lower faults) relate to the outputs (higher faults) through gates



# FAULT TREE EVENT SYMBOLS

## Gate Symbols



OR gate



AND gate

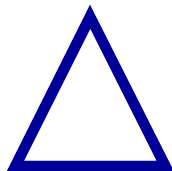


Priority AND gate

## Other Symbols

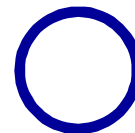


Remarks

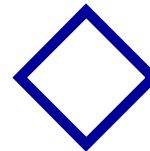


Transfer

## Primary Event Symbols



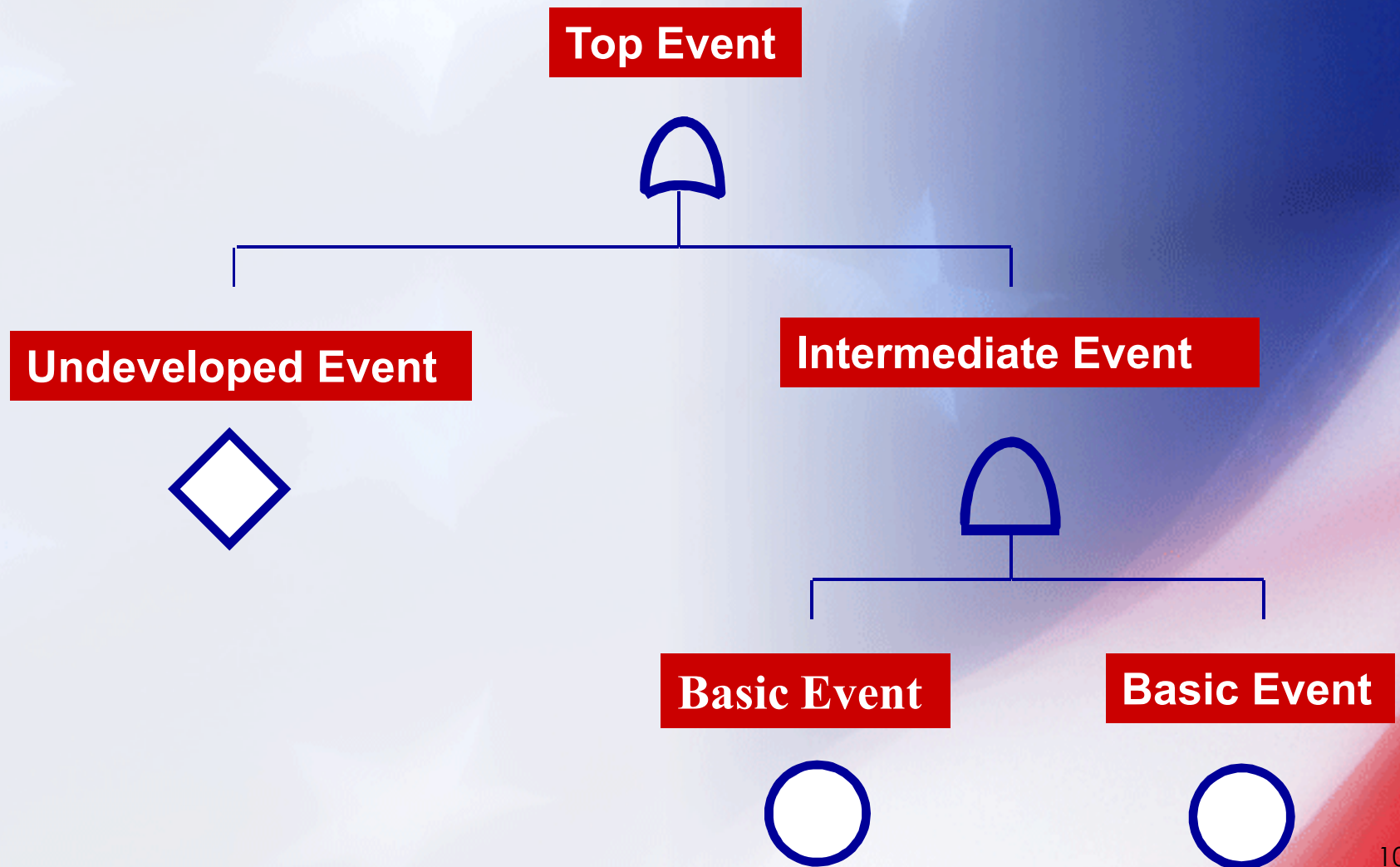
Basic event



Undeveloped event

**Advanced Features:**  
**NAND, NOR, XOR,**  
**NOT, Voting gates,**  
**Inhibit gates, Sequence**  
**Enforcing gates**

# FAULT TREE STRUCTURE





# FAULT TREE CONSTRUCTION - GENERAL

**Completeness (and value) in fault tree  
construction is achieved by:**

- Thorough understanding of the system
- Thoughtful definition of top event
- Careful definition of each fault
- Taking small steps in logic
- Being exhaustive at each step

**Avoid:**

**“That could never happen”**

**“We never had a failure/fault before”**

**Failure Space vs. Success Space**  
**Red Thinking vs. Blue Thinking**

# TOP EVENT DEFINITION

Process begins by defining the Top Event in the fault tree diagram and working down from there . After the fault tree top event is defined:

**Unacceptable Consequences**

- Analyst determines the immediate, necessary and sufficient causes for the top event occurrence
- Continue identifying the immediate, necessary and sufficient causes until all faults have been resolved into their elementary faults or failures
- Usually quit at a level of detail where features are identifiable, controllable, or easily measurable
  - ▶ Hydraulic coupler vs. coupler metallic composition
  - ▶ Pressure regulator vs. internal parts

**Controls**



# FAULT TREE EVALUATION - CUT SETS

- Solution of the fault tree provides the “*cut set expression*”
  - ▶ Cut set - any combination of basic events that is sufficient to cause the top event to occur
  - ▶ Minimal cut set - any combination of primary events that is necessary and sufficient to cause the top event to occur
    - Redundancy has been eliminated
  - ▶ First-order fault (Single Point Failure) – a minimal cut set containing only one event.
    - This single basic event is sufficient to cause system failure
    - “OR GATE” rule of thumb

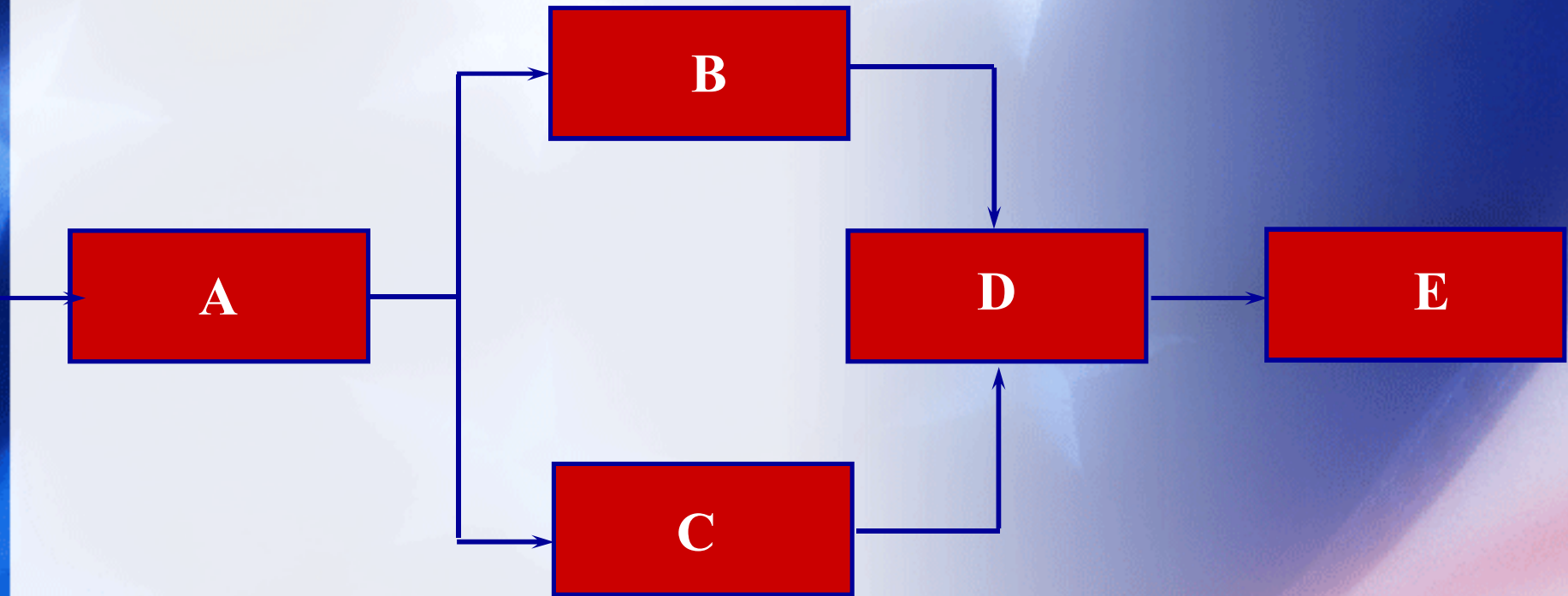
## **Note:**

**Second-order cut sets containing only administrative controls may be of greater concern than having an engineered control first-order fault**

## **Note:**

**A Basic Event reoccurring in several Multi-order cut sets indicates importance of that Basic Event**

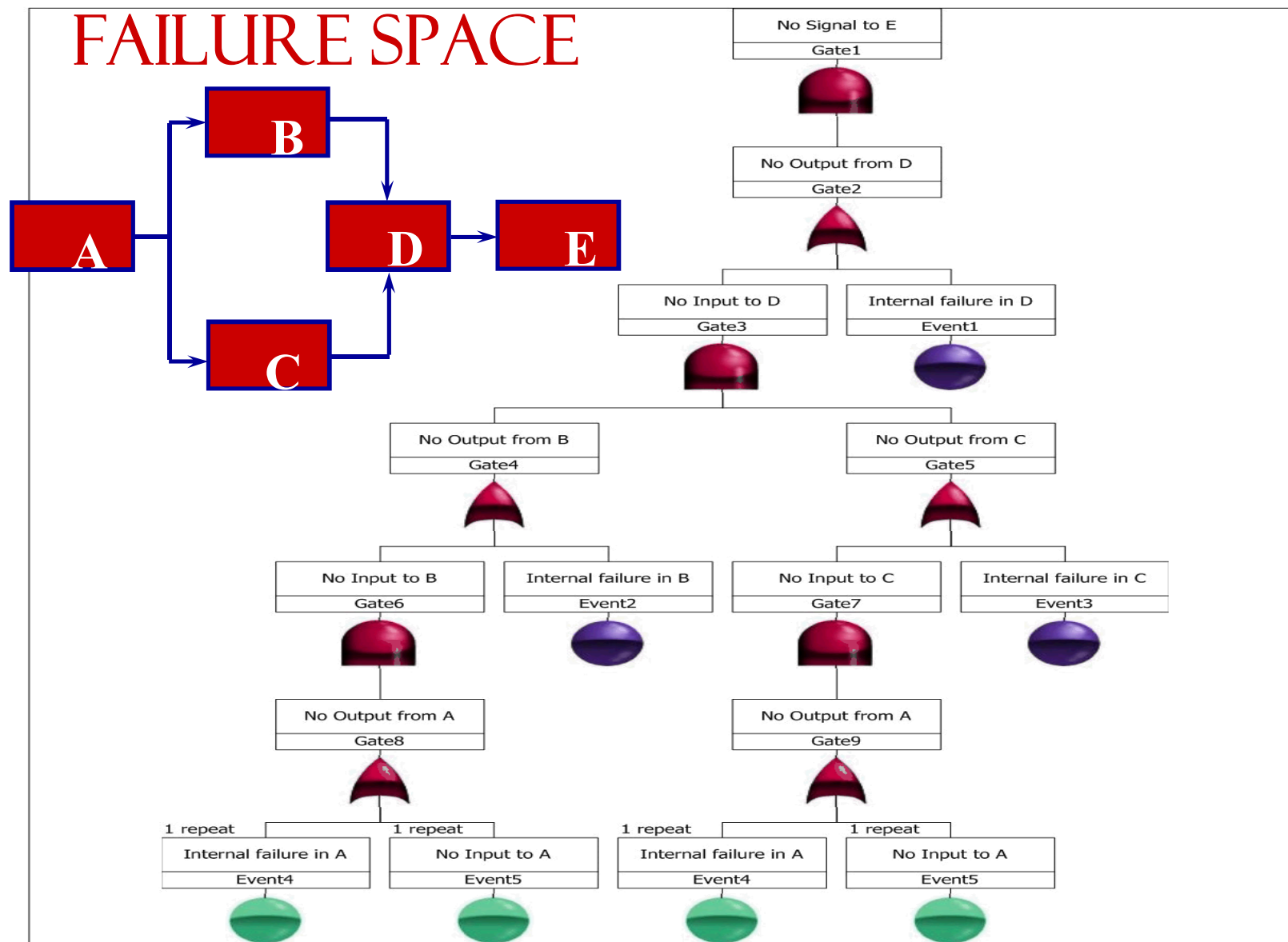
# EXAMPLE SYSTEM DIAGRAM



**Success Space:** An input signal to **A** provides an output to **B** and **C**. An output from **B** and/or **C** produces a signal from **D** which finally passes a signal to **E**.



# FAILURE SPACE



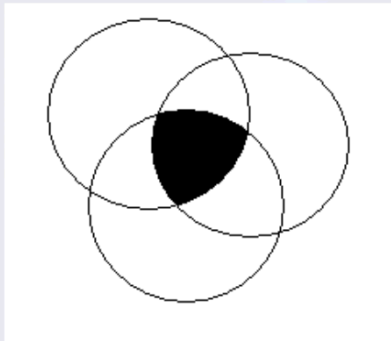
# SET THEORY / BOOLEAN ALGEBRA

- The software does this all for us
  - ▶ It's been independently V&V'd
- I'll breeze through this part just to let you know how it's done.
  - ▶ Write Boolean equations
  - ▶ Substitute to get system equation
  - ▶ Reduce equations using theorems and identities
  - ▶ Find cut sets and their importance



# SET THEORY

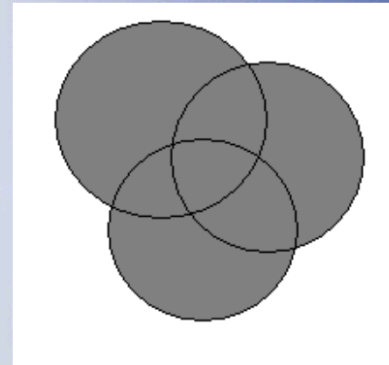
## “Intersection” Operation



$$X \cap Y \cap Z$$

$$X \bullet Y \bullet Z$$

## “Union” Operation



$$X \cup Y \cup Z$$

$$X + Y + Z$$

<u>Operation</u>	<u>Probability</u>	<u>Mathematics</u>	<u>Engineering</u>
Union	A or B	$A \cup B$	$A + B$
Intersection	A and B	$A \cap B$	$A \bullet B$ or $AB$

# FAULT TREE CUT SET SOLUTION

## Step 1: Generate one equation

for each intermediate event

in fault tree (eight intermediate events)

Gate1 = Gate2

Gate 2 = Gate 3 + Event 1

Gate 3 = Gate 4 • Gate 5

Gate 4 = Gate 6 + Event 2

Gate 5 = Event 3 + Gate 7

Gate 6 = Gate 8

Gate 7 = Gate 9

Gate 8 = Event 4 + Event 5

Gate 9 = Event 4 + Event 5

Gate 1 = No Signal from E

Gate 2 = No Output from D

Gate 3 = No Input to D

Gate 4 = No Output from B

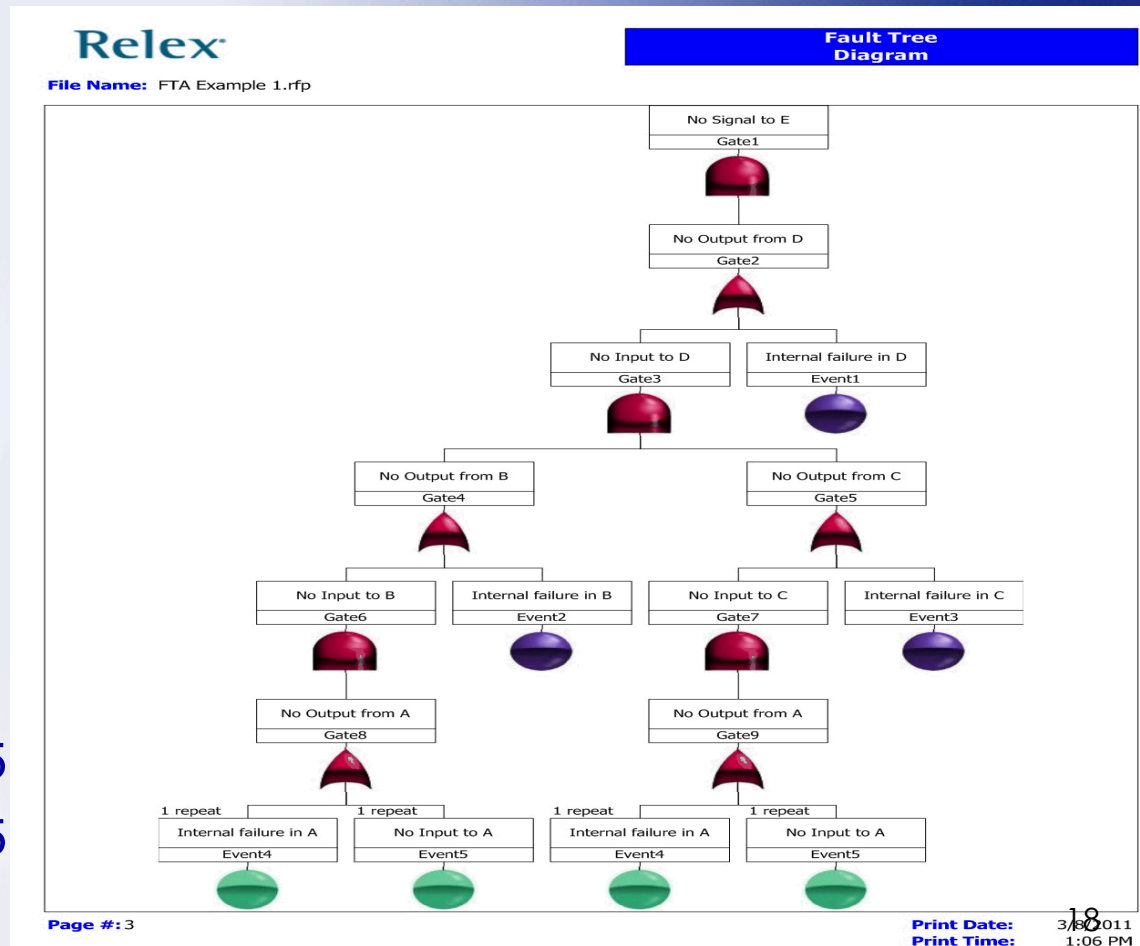
Gate 5 = No Output from C

Gate 6 = No Input to B

Gate 7 = No Input to C

Gate 8 = No Output from A

Gate 9 = No Output from A



# FAULT TREE CUT SET SOLUTION (CONT.)

**Step 2:** Generate the top event equation and substitute the equations that define the intermediate events

$$\text{Gate 1} = \text{Gate 2}$$

$$= \text{Gate 3} + \text{Event 1}$$

$$= (\text{Gate 4} \cdot \text{Gate 5}) + \text{Event 1}$$

$$= (\text{Gate 6} + \text{Event 2}) \cdot (\text{Gate 7} + \text{Event 3}) + \text{Event 1}$$

$$= (\text{Gate 8} + \text{Event 2}) \cdot (\text{Gate 9} + \text{Event 3}) + \text{Event 1}$$

$$= ((\text{Event 4} + \text{Event 5}) + \text{Event 2}) \cdot ((\text{Event 4} + \text{Event 5}) + \text{Event 3}) + \text{Event 1}$$



# FAULT TREE CUT SET SOLUTION (CONT.)

**Step 3:** Expand the equation using the distributive and associative laws:

$$\begin{aligned}\text{Gate 1} &= ((\text{Event 4} + \text{Event 5}) + \text{Event 2}) \cdot ((\text{Event 4} + \text{Event 5}) + \text{Event 3}) + \text{Event 1} \\ &= (\text{Event 4} + \text{Event 5} + \text{Event 2}) \cdot (\text{Event 4} + \text{Event 5} + \text{Event 3}) + \text{Event 1} \\ &= \text{Event 4} \cdot \text{Event 4} + \text{Event 4} \cdot \text{Event 5} + \text{Event 4} \cdot \text{Event 3} + \text{Event 5} \cdot \text{Event 4} + \text{Event 5} \cdot \text{Event 5} + \text{Event 5} \cdot \text{Event 3} + \text{Event 2} \cdot \text{Event 4} + \text{Event 2} \cdot \text{Event 5} + \text{Event 2} \cdot \text{Event 3} + \text{Event 1}\end{aligned}$$

# FAULT TREE CUT SET SOLUTION (CONT.)

**Step 4:** Minimize the expression using  $P \cdot P = P$   
and  $P + (P \cdot Q) = P$

- ▶ Cut sets reduced using  $P \cdot P = P$ :
  - Intersection of a set with itself is the set
  - Union of a set with itself is the set

Event 4 • Event 4 = Event 4

Event 5 • Event 5 = Event 5

- ▶ Cut sets further reduced using  $P + (P \cdot Q) = P$ ;  
for example:

- Union of set with a subset of that set is the set

Event 4 + Event 4 • Event 5 = Event 4

- Following reduction using identities, the  
minimal cut sets remain comprised of basic  
events

# EXAMPLE FAULT TREE CUT SETS

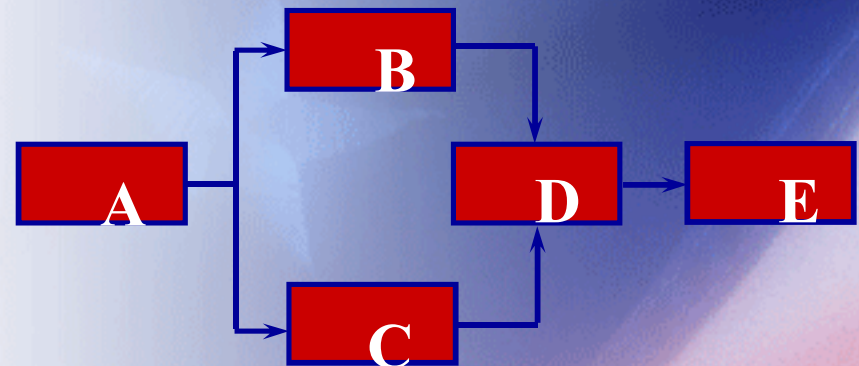
## Top Event Equation:

Gate 1 = Event 5 + Event 4 + Event 1 + Event 3 • Event 2.

Gate 1 = Event 5 OR Event 4 OR Event 1 OR (Event 3 AND Event 2)

## Individual minimal cut sets:

Event 5	(No input to A)
Event 4	(Internal failure in A)
Event 1	(Internal failure in D)
Event 3 • Event 2	(Internal failure in B and Internal failure in C)





# FAULT TREE MANUAL SOLUTION AND QUANTIFICATION

- Assigning the following basic event probabilities (no units specified):

Event 5 =  $1\text{E-}4$  (no input to A)  $1/10000$

Event 4 =  $5\text{E-}3$  (Internal failure to A)  $5/1000$

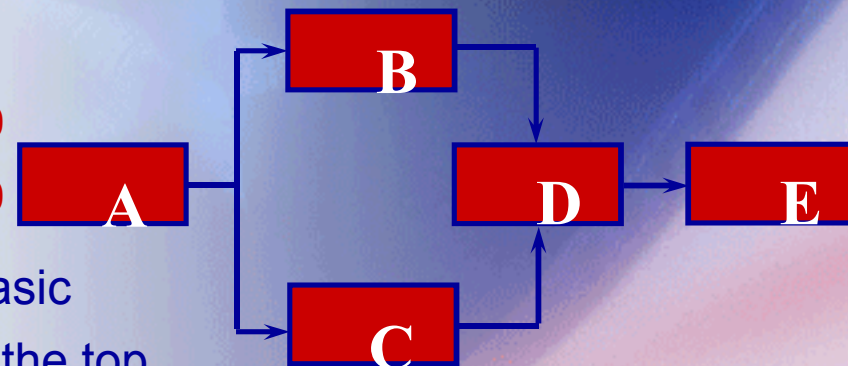
Event 2 =  $1\text{E-}1$  (Internal failure to B)  $1/10$

Event 3 =  $8\text{E-}3$  (Internal failure to C)  $8/1000$

Event 1 =  $3\text{E-}3$  (Internal failure to D)  $3/1000$

- Cut sets are quantified, assuming the basic event occurrences are independent, for the top event probability:

$$\begin{aligned} P(\text{No signal to E}) &= 1\text{E-}4 + 5\text{E-}3 + 3\text{E-}3 + 1\text{E-}1 \cdot 8\text{E-}3 \\ &= 8.9\text{E-}3 \end{aligned}$$



# CUT SET IMPORTANCE

- Relative cut set importance is the ratio of the minimal cut set probability to the total system top event probability

- Cut Set

## Importance

Event 5 (No input to A)	1.1%
Event 4 (Internal failure in A)	56.2%
Event 1 (Internal failure in D)	33.7%
Event 3 • Event 2 (I.F. in B&C)	9.0%

**Event 5 = 1E-4 (no input to A)**

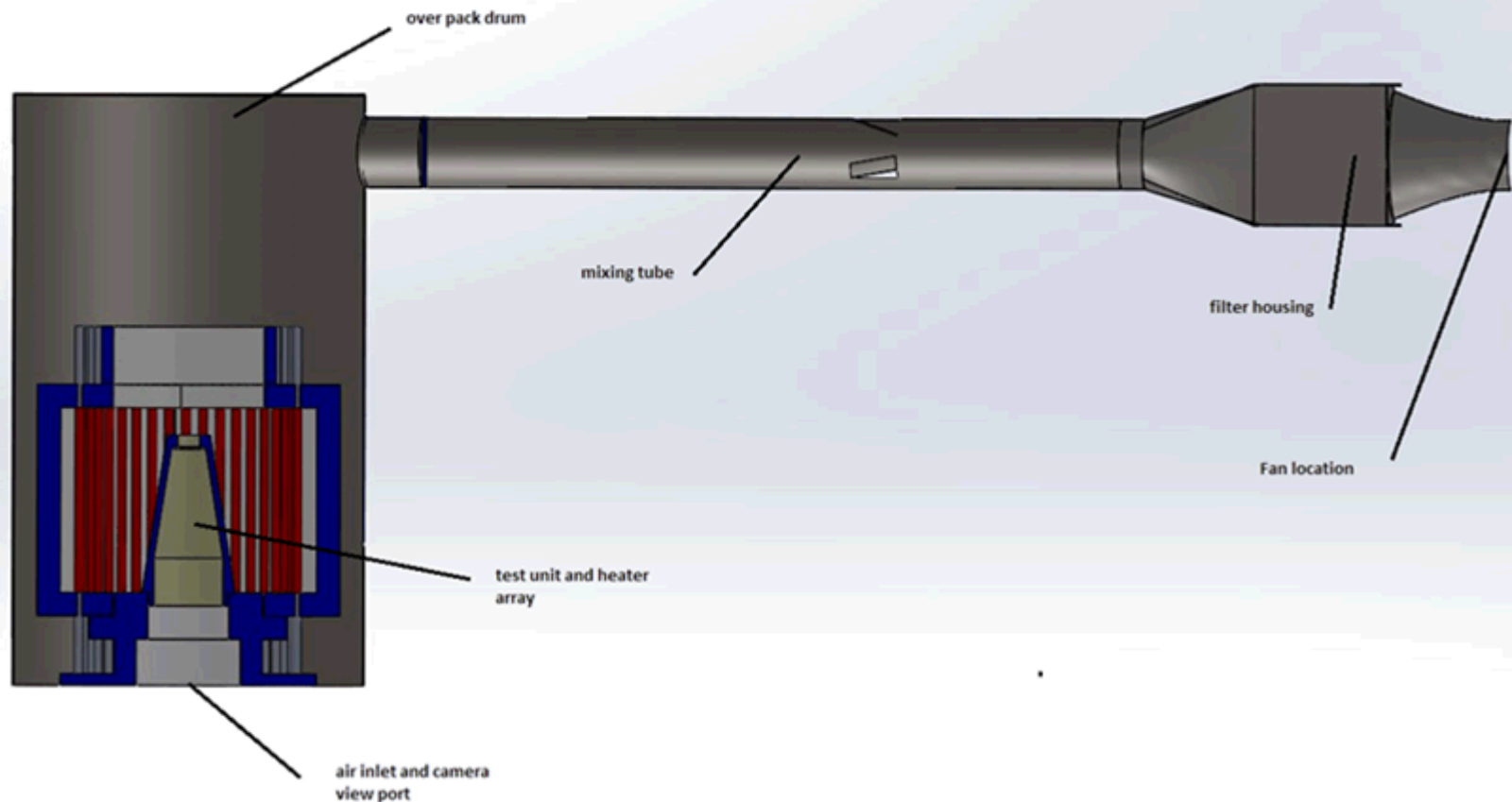
**Event 4 = 5E-3 (Internal failure to A)**

**Event 2 = 1E-1 (Internal failure to B)**

**Event 3 = 8E-3 (Internal failure to C)**

**Event 1 = 3E-3 (Internal failure to D)**

# CONE THERMAL TEST (PRE-FTA)



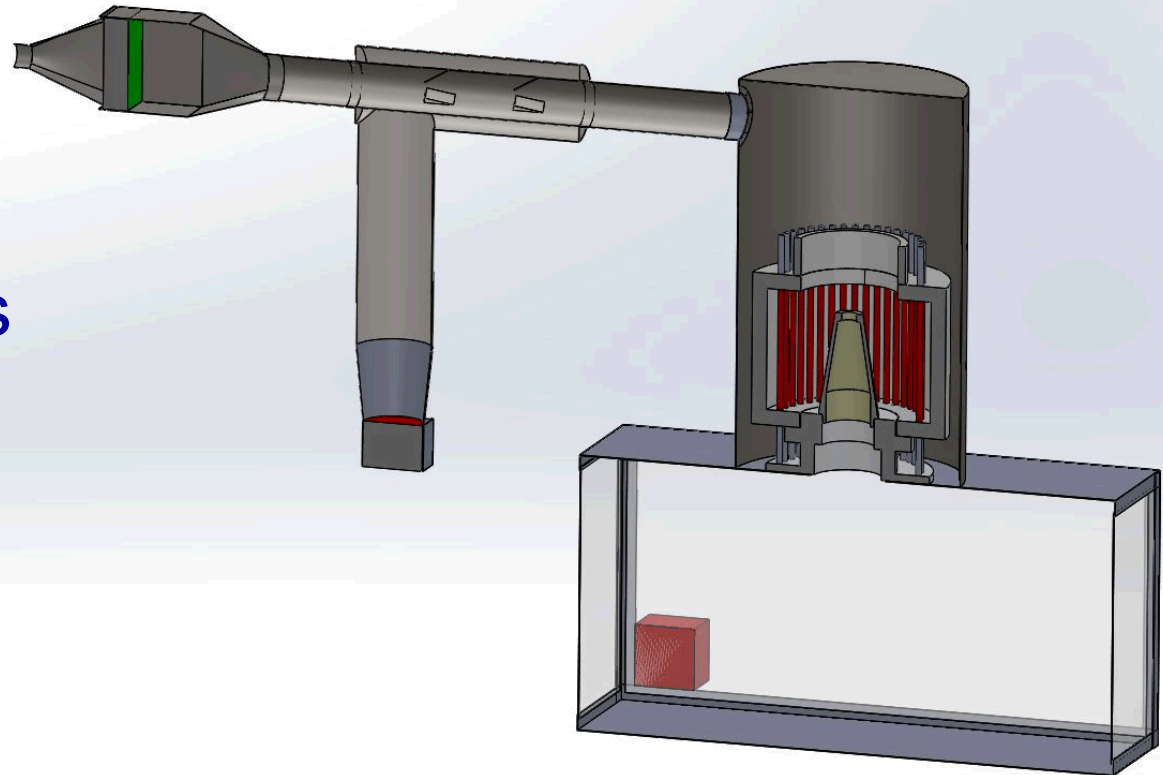


# CUTSET RESULTS:

- Several First-Order fault identified
  - ▶ Asbestos containment is fine only if everything works properly
  - ▶ Intended openings in the system are potential paths for release of asbestos
    - Air inlet at the bottom
    - Mixing ports to cool air prior to filter
  - ▶ Many possible fan faults could would force asbestos out of air inlet and mixing ports
    - Failure of power to fan (common at TTC)
    - Fan motor failure, shaft failure, etc.
  - ▶ Exit filter or seal failure
    - Mitigated by proper selection of filter, installation, and independent inspection by qualified contractor

# CONE THERMAL TEST (POST-FTA)

- UPS added to fan system
- Mixing ports covered
- Air inlet covered



# ENGINEERED SAFETY / FTA RESULTS

- FTA provided a formal method to evaluate the safety of the design and support the safety case
- First order faults / Single-point failures identified
  - ▶ Eliminated through redesign
  - ▶ Mitigated
    - Large design margins
    - Independently inspected
- Some second-order cutsets eliminated
  - ▶ Example: If both facility power and UPS fail, asbestos remains contained
- Initial FTA performed in one day. Redesign to eliminate issues done the day after
  - ▶ Test delayed by two weeks because of additional parts, assembly, and inspection
  - ▶ Lesson Learned: Have FTA done earlier rather than later
- FTA does not have to be labor intensive and is beneficial even for simple systems



# RESOURCES

- Software:
  - ▶ PTC Windchill software
  - ▶ Isograph
  - ▶ INL's Sapphire
  - ▶ Reliasoft
  - ▶ Itemsoft FTA
- Some provide trial versions
  - ▶ Limited time
  - ▶ Limited number of gates
  - ▶ Limited number of levels
- User groups
  - ▶ Poor customer service on the few I've used